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# Statistics for Business & Economics <sup>13e</sup>



# Statistics for Business & Economics

13e

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*Dedicated to  
Marcia, Cherri, Robbie, Karen, and Teresa*



# Brief Contents

<b>Preface</b>	<b>xxiii</b>
<b>About the Authors</b>	<b>xxix</b>
<b>Chapter 1</b>	<b>Data and Statistics 1</b>
<b>Chapter 2</b>	<b>Descriptive Statistics: Tabular and Graphical Displays 32</b>
<b>Chapter 3</b>	<b>Descriptive Statistics: Numerical Measures 102</b>
<b>Chapter 4</b>	<b>Introduction to Probability 171</b>
<b>Chapter 5</b>	<b>Discrete Probability Distributions 217</b>
<b>Chapter 6</b>	<b>Continuous Probability Distributions 269</b>
<b>Chapter 7</b>	<b>Sampling and Sampling Distributions 302</b>
<b>Chapter 8</b>	<b>Interval Estimation 346</b>
<b>Chapter 9</b>	<b>Hypothesis Tests 385</b>
<b>Chapter 10</b>	<b>Inference About Means and Proportions with Two Populations 443</b>
<b>Chapter 11</b>	<b>Inferences About Population Variances 483</b>
<b>Chapter 12</b>	<b>Comparing Multiple Proportions, Test of Independence and Goodness of Fit 507</b>
<b>Chapter 13</b>	<b>Experimental Design and Analysis of Variance 544</b>
<b>Chapter 14</b>	<b>Simple Linear Regression 598</b>
<b>Chapter 15</b>	<b>Multiple Regression 681</b>
<b>Chapter 16</b>	<b>Regression Analysis: Model Building 754</b>
<b>Chapter 17</b>	<b>Time Series Analysis and Forecasting 805</b>
<b>Chapter 18</b>	<b>Nonparametric Methods 871</b>
<b>Chapter 19</b>	<b>Statistical Methods for Quality Control 916</b>
<b>Chapter 20</b>	<b>Index Numbers 950</b>
<b>Chapter 21</b>	<b>Decision Analysis (On Website)</b>
<b>Chapter 22</b>	<b>Sample Survey (On Website)</b>
<b>Appendix A</b>	<b>References and Bibliography 972</b>
<b>Appendix B</b>	<b>Tables 974</b>
<b>Appendix C</b>	<b>Summation Notation 1001</b>
<b>Appendix D</b>	<b>Self-Test Solutions and Answers to Even-Numbered Exercises 1003</b>
<b>Appendix E</b>	<b>Microsoft Excel 2013 and Tools for Statistical Analysis 1070</b>
<b>Appendix F</b>	<b>Computing <math>p</math>-Values Using Minitab and Excel 1078</b>
<b>Index</b>	<b>1082</b>





# Contents

<b>Preface</b>	<b>xxiii</b>
<b>About the Authors</b>	<b>xxix</b>

## **Chapter 1** Data and Statistics 1

### **Statistics in Practice: Bloomberg Businessweek** 2

#### **1.1 Applications in Business and Economics** 3

Accounting	3
Finance	4
Marketing	4
Production	4
Economics	4
Information Systems	5

#### **1.2 Data** 5

Elements, Variables, and Observations	5
Scales of Measurement	7
Categorical and Quantitative Data	8
Cross-Sectional and Time Series Data	8

#### **1.3 Data Sources** 11

Existing Sources	11
Observational Study	12
Experiment	13
Time and Cost Issues	13
Data Acquisition Errors	13

#### **1.4 Descriptive Statistics** 14

#### **1.5 Statistical Inference** 16

#### **1.6 Analytics** 17

#### **1.7 Big Data and Data Mining** 18

#### **1.8 Computers and Statistical Analysis** 20

#### **1.9 Ethical Guidelines for Statistical Practice** 20

#### **Summary** 22

#### **Glossary** 23

#### **Supplementary Exercises** 24

## **Chapter 2** Descriptive Statistics: Tabular and Graphical Displays 32

### **Statistics in Practice: Colgate-Palmolive Company** 33

#### **2.1 Summarizing Data for a Categorical Variable** 34

Frequency Distribution	34
------------------------	----

	Relative Frequency and Percent Frequency Distributions	35
	Bar Charts and Pie Charts	35
<b>2.2</b>	<b>Summarizing Data for a Quantitative Variable</b>	<b>41</b>
	Frequency Distribution	41
	Relative Frequency and Percent Frequency Distributions	43
	Dot Plot	43
	Histogram	44
	Cumulative Distributions	45
	Stem-and-Leaf Display	46
<b>2.3</b>	<b>Summarizing Data for Two Variables Using Tables</b>	<b>55</b>
	Crosstabulation	55
	Simpson's Paradox	58
<b>2.4</b>	<b>Summarizing Data for Two Variables Using Graphical Displays</b>	<b>64</b>
	Scatter Diagram and Trendline	64
	Side-by-Side and Stacked Bar Charts	65
<b>2.5</b>	<b>Data Visualization: Best Practices in Creating Effective Graphical Displays</b>	<b>71</b>
	Creating Effective Graphical Displays	71
	Choosing the Type of Graphical Display	72
	Data Dashboards	72
	Data Visualization in Practice: Cincinnati Zoo and Botanical Garden	74
	<b>Summary</b>	<b>77</b>
	<b>Glossary</b>	<b>78</b>
	<b>Key Formulas</b>	<b>79</b>
	<b>Supplementary Exercises</b>	<b>79</b>
	<b>Case Problem 1 Pelican Stores</b>	<b>84</b>
	<b>Case Problem 2 Motion Picture Industry</b>	<b>85</b>
	<b>Case Problem 3 Queen City</b>	<b>86</b>
	<b>Appendix 2.1 Using Minitab for Tabular and Graphical Presentations</b>	<b>87</b>
	<b>Appendix 2.2 Using Excel for Tabular and Graphical Presentations</b>	<b>90</b>
	<b>Chapter 3 Descriptive Statistics: Numerical Measures</b>	<b>102</b>
	<b>Statistics in Practice: Small Fry Design</b>	<b>103</b>
<b>3.1</b>	<b>Measures of Location</b>	<b>104</b>
	Mean	104
	Weighted Mean	106
	Median	107
	Geometric Mean	109
	Mode	110
	Percentiles	111
	Quartiles	112

<b>3.2 Measures of Variability</b>	<b>118</b>
Range	118
Interquartile Range	119
Variance	119
Standard Deviation	120
Coefficient of Variation	121
<b>3.3 Measures of Distribution Shape, Relative Location, and Detecting Outliers</b>	<b>125</b>
Distribution Shape	125
z-Scores	125
Chebyshev's Theorem	127
Empirical Rule	128
Detecting Outliers	130
<b>3.4 Five-Number Summaries and Box Plots</b>	<b>133</b>
Five-Number Summary	133
Box Plot	134
Comparative Analysis Using Box Plots	135
<b>3.5 Measures of Association Between Two Variables</b>	<b>138</b>
Covariance	138
Interpretation of the Covariance	140
Correlation Coefficient	141
Interpretation of the Correlation Coefficient	144
<b>3.6 Data Dashboards: Adding Numerical Measures to Improve Effectiveness</b>	<b>148</b>
<b>Summary</b>	<b>151</b>
<b>Glossary</b>	<b>152</b>
<b>Key Formulas</b>	<b>153</b>
<b>Supplementary Exercises</b>	<b>155</b>
<b>Case Problem 1 Pelican Stores</b>	<b>160</b>
<b>Case Problem 2 Motion Picture Industry</b>	<b>161</b>
<b>Case Problem 3 Business Schools of Asia-Pacific</b>	<b>162</b>
<b>Case Problem 4 Heavenly Chocolates Website Transactions</b>	<b>164</b>
<b>Case Problem 5 African Elephant Populations</b>	<b>165</b>
<b>Appendix 3.1 Descriptive Statistics Using Minitab</b>	<b>166</b>
<b>Appendix 3.2 Descriptive Statistics Using Excel</b>	<b>168</b>

## **Chapter 4 Introduction to Probability 171**

### **Statistics in Practice: National Aeronautics and Space Administration 172**

#### **4.1 Random Experiments, Counting Rules, and Assigning Probabilities 173**

Counting Rules, Combinations, and Permutations 174

Assigning Probabilities 178

Probabilities for the KP&L Project 180

#### **4.2 Events and Their Probabilities 183**

**4.3 Some Basic Relationships of Probability 187**

Complement of an Event 187

Addition Law 188

**4.4 Conditional Probability 194**

Independent Events 197

Multiplication Law 197

**4.5 Bayes' Theorem 202**

Tabular Approach 205

**Summary 208****Glossary 208****Key Formulas 209****Supplementary Exercises 210****Case Problem Hamilton County Judges 214****Chapter 5 Discrete Probability Distributions 217****Statistics in Practice: Citibank 218****5.1 Random Variables 219**

Discrete Random Variables 219

Continuous Random Variables 220

**5.2 Developing Discrete Probability Distributions 222****5.3 Expected Value and Variance 227**

Expected Value 227

Variance 227

**5.4 Bivariate Distributions, Covariance, and Financial Portfolios 232**

A Bivariate Empirical Discrete Probability Distribution 232

Financial Applications 235

Summary 238

**5.5 Binomial Probability Distribution 241**

A Binomial Experiment 242

Martin Clothing Store Problem 243

Using Tables of Binomial Probabilities 247

Expected Value and Variance for the Binomial Distribution 248

**5.6 Poisson Probability Distribution 252**

An Example Involving Time Intervals 253

An Example Involving Length or Distance Intervals 254

**5.7 Hypergeometric Probability Distribution 256****Summary 259****Glossary 260****Key Formulas 261****Supplementary Exercises 262****Case Problem *Go Bananas!* 266****Appendix 5.1 Discrete Probability Distributions with Minitab 267****Appendix 5.2 Discrete Probability Distributions with Excel 267**

## **Chapter 6** Continuous Probability Distributions 269

### **Statistics in Practice: Procter & Gamble 270**

#### **6.1 Uniform Probability Distribution 271**

Area as a Measure of Probability 272

#### **6.2 Normal Probability Distribution 275**

Normal Curve 275

Standard Normal Probability Distribution 277

Computing Probabilities for Any Normal Probability Distribution 282

Great Tire Company Problem 283

#### **6.3 Normal Approximation of Binomial Probabilities 287**

#### **6.4 Exponential Probability Distribution 291**

Computing Probabilities for the Exponential Distribution 291

Relationship Between the Poisson and Exponential Distributions 292

### **Summary 294**

### **Glossary 295**

### **Key Formulas 295**

### **Supplementary Exercises 296**

### **Case Problem Specialty Toys 299**

### **Appendix 6.1 Continuous Probability Distributions with Minitab 300**

### **Appendix 6.2 Continuous Probability Distributions with Excel 301**

## **Chapter 7** Sampling and Sampling Distributions 302

### **Statistics in Practice: Meadwestvaco Corporation 303**

#### **7.1 The Electronics Associates Sampling Problem 304**

#### **7.2 Selecting a Sample 305**

Sampling from a Finite Population 305

Sampling from an Infinite Population 307

#### **7.3 Point Estimation 310**

Practical Advice 312

#### **7.4 Introduction to Sampling Distributions 314**

#### **7.5 Sampling Distribution of $\bar{x}$ 316**

Expected Value of  $\bar{x}$  317

Standard Deviation of  $\bar{x}$  317

Form of the Sampling Distribution of  $\bar{x}$  318

Sampling Distribution of  $\bar{x}$  for the EAI Problem 319

Practical Value of the Sampling Distribution of  $\bar{x}$  320

Relationship Between the Sample Size and the Sampling Distribution of  $\bar{x}$  322

#### **7.6 Sampling Distribution of $\bar{p}$ 326**

Expected Value of  $\bar{p}$  327

Standard Deviation of  $\bar{p}$  327

Form of the Sampling Distribution of  $\bar{p}$  328

Practical Value of the Sampling Distribution of  $\bar{p}$  329

<b>7.7 Properties of Point Estimators</b>	<b>332</b>
Unbiased	332
Efficiency	333
Consistency	334
<b>7.8 Other Sampling Methods</b>	<b>335</b>
Stratified Random Sampling	335
Cluster Sampling	335
Systematic Sampling	336
Convenience Sampling	336
Judgment Sampling	337
<b>Summary</b>	<b>337</b>
<b>Glossary</b>	<b>338</b>
<b>Key Formulas</b>	<b>339</b>
<b>Supplementary Exercises</b>	<b>339</b>
<b>Case Problem Marion Dairies</b>	<b>342</b>
<b>Appendix 7.1 The Expected Value and Standard Deviation of <math>\bar{x}</math></b>	<b>342</b>
<b>Appendix 7.2 Random Sampling with Minitab</b>	<b>344</b>
<b>Appendix 7.3 Random Sampling with Excel</b>	<b>345</b>
<b>Chapter 8 Interval Estimation</b>	<b>346</b>
<b>Statistics in Practice: Food Lion</b>	<b>347</b>
<b>8.1 Population Mean: <math>\sigma</math> Known</b>	<b>348</b>
Margin of Error and the Interval Estimate	348
Practical Advice	352
<b>8.2 Population Mean: <math>\sigma</math> Unknown</b>	<b>354</b>
Margin of Error and the Interval Estimate	355
Practical Advice	358
Using a Small Sample	358
Summary of Interval Estimation Procedures	360
<b>8.3 Determining the Sample Size</b>	<b>363</b>
<b>8.4 Population Proportion</b>	<b>366</b>
Determining the Sample Size	368
<b>Summary</b>	<b>372</b>
<b>Glossary</b>	<b>373</b>
<b>Key Formulas</b>	<b>373</b>
<b>Supplementary Exercises</b>	<b>374</b>
<b>Case Problem 1 <i>Young Professional</i> Magazine</b>	<b>377</b>
<b>Case Problem 2 Gulf Real Estate Properties</b>	<b>378</b>
<b>Case Problem 3 Metropolitan Research, Inc.</b>	<b>378</b>
<b>Appendix 8.1 Interval Estimation with Minitab</b>	<b>380</b>
<b>Appendix 8.2 Interval Estimation Using Excel</b>	<b>382</b>

## **Chapter 9 Hypothesis Tests 385**

### **Statistics in Practice: John Morrell & Company 386**

#### **9.1 Developing Null and Alternative Hypotheses 387**

The Alternative Hypothesis as a Research Hypothesis 387

The Null Hypothesis as an Assumption to Be Challenged 388

Summary of Forms for Null and Alternative Hypotheses 389

#### **9.2 Type I and Type II Errors 390**

#### **9.3 Population Mean: $\sigma$ Known 393**

One-Tailed Test 393

Two-Tailed Test 399

Summary and Practical Advice 401

Relationship Between Interval Estimation and Hypothesis Testing 403

#### **9.4 Population Mean: $\sigma$ Unknown 408**

One-Tailed Test 408

Two-Tailed Test 409

Summary and Practical Advice 411

#### **9.5 Population Proportion 414**

Summary 416

#### **9.6 Hypothesis Testing and Decision Making 419**

#### **9.7 Calculating the Probability of Type II Errors 420**

#### **9.8 Determining the Sample Size for a Hypothesis Test About a Population Mean 425**

#### **Summary 428**

#### **Glossary 429**

#### **Key Formulas 430**

#### **Supplementary Exercises 430**

#### **Case Problem 1 Quality Associates, Inc. 433**

#### **Case Problem 2 Ethical Behavior of Business Students at Bayview University 435**

#### **Appendix 9.1 Hypothesis Testing with Minitab 436**

#### **Appendix 9.2 Hypothesis Testing with Excel 438**

## **Chapter 10 Inference About Means and Proportions with Two Populations 443**

### **Statistics in Practice: U.S. Food and Drug Administration 444**

#### **10.1 Inferences About the Difference Between Two Population Means: $\sigma_1$ and $\sigma_2$ Known 445**

Interval Estimation of  $\mu_1 - \mu_2$  445

Hypothesis Tests About  $\mu_1 - \mu_2$  447

Practical Advice 449

#### **10.2 Inferences About the Difference Between Two Population Means: $\sigma_1$ and $\sigma_2$ Unknown 452**

Interval Estimation of  $\mu_1 - \mu_2$  452

Hypothesis Tests About $\mu_1 - \mu_2$	454
Practical Advice	456
<b>10.3 Inferences About the Difference Between Two Population Means:     Matched Samples</b>	<b>460</b>
<b>10.4 Inferences About the Difference Between Two Population Proportions</b>	<b>466</b>
Interval Estimation of $p_1 - p_2$	466
Hypothesis Tests About $p_1 - p_2$	468
<b>Summary</b>	<b>472</b>
<b>Glossary</b>	<b>472</b>
<b>Key Formulas</b>	<b>473</b>
<b>Supplementary Exercises</b>	<b>474</b>
<b>Case Problem Par, Inc.</b>	<b>477</b>
<b>Appendix 10.1 Inferences About Two Populations Using Minitab</b>	<b>478</b>
<b>Appendix 10.2 Inferences About Two Populations Using Excel</b>	<b>480</b>
<b>Chapter 11 Inferences About Population Variances</b>	<b>483</b>
<b>Statistics in Practice: U.S. Government Accountability Office</b>	<b>484</b>
<b>11.1 Inferences About a Population Variance</b>	<b>485</b>
Interval Estimation	485
Hypothesis Testing	489
<b>11.2 Inferences About Two Population Variances</b>	<b>495</b>
<b>Summary</b>	<b>502</b>
<b>Key Formulas</b>	<b>502</b>
<b>Supplementary Exercises</b>	<b>502</b>
<b>Case Problem Air Force Training Program</b>	<b>504</b>
<b>Appendix 11.1 Population Variances with Minitab</b>	<b>505</b>
<b>Appendix 11.2 Population Variances with Excel</b>	<b>506</b>
<b>Chapter 12 Comparing Multiple Proportions, Test of Independence     and Goodness of Fit</b>	<b>507</b>
<b>Statistics in Practice: United Way</b>	<b>508</b>
<b>12.1 Testing the Equality of Population Proportions for Three     or More Populations</b>	<b>509</b>
A Multiple Comparison Procedure	514
<b>12.2 Test of Independence</b>	<b>519</b>
<b>12.3 Goodness of Fit Test</b>	<b>527</b>
Multinomial Probability Distribution	527
Normal Probability Distribution	530
<b>Summary</b>	<b>536</b>
<b>Glossary</b>	<b>536</b>
<b>Key Formulas</b>	<b>537</b>
<b>Supplementary Exercises</b>	<b>537</b>



**Case Problem A Bipartisan Agenda for Change 540**

**Appendix 12.1 Chi-Square Tests Using Minitab 541**

**Appendix 12.2 Chi-Square Tests Using Excel 542**

## **Chapter 13 Experimental Design and Analysis of Variance 544**

**Statistics in Practice: Burke Marketing Services, Inc. 545**

**13.1 An Introduction to Experimental Design and Analysis of Variance 546**

Data Collection 547

Assumptions for Analysis of Variance 548

Analysis of Variance: A Conceptual Overview 548

**13.2 Analysis of Variance and the Completely Randomized Design 551**

Between-Treatments Estimate of Population Variance 552

Within-Treatments Estimate of Population Variance 553

Comparing the Variance Estimates: The  $F$  Test 554

ANOVA Table 556

Computer Results for Analysis of Variance 557

Testing for the Equality of  $k$  Population Means:  
An Observational Study 558

**13.3 Multiple Comparison Procedures 562**

Fisher's LSD 562

Type I Error Rates 565

**13.4 Randomized Block Design 568**

Air Traffic Controller Stress Test 569

ANOVA Procedure 570

Computations and Conclusions 571

**13.5 Factorial Experiment 575**

ANOVA Procedure 577

Computations and Conclusions 577

**Summary 582**

**Glossary 583**

**Key Formulas 583**

**Supplementary Exercises 586**

**Case Problem 1 Wentworth Medical Center 590**

**Case Problem 2 Compensation for Sales Professionals 591**

**Appendix 13.1 Analysis of Variance with Minitab 592**

**Appendix 13.2 Analysis of Variance with Excel 594**

## **Chapter 14 Simple Linear Regression 598**

**Statistics in Practice: Alliance Data Systems 599**

**14.1 Simple Linear Regression Model 600**

Regression Model and Regression Equation 600

Estimated Regression Equation 601

<b>14.2</b>	<b>Least Squares Method</b>	<b>603</b>
<b>14.3</b>	<b>Coefficient of Determination</b>	<b>614</b>
	Correlation Coefficient	617
<b>14.4</b>	<b>Model Assumptions</b>	<b>621</b>
<b>14.5</b>	<b>Testing for Significance</b>	<b>622</b>
	Estimate of $\sigma^2$	623
	$t$ Test	623
	Confidence Interval for $\beta_1$	625
	$F$ Test	626
	Some Cautions About the Interpretation of Significance Tests	628
<b>14.6</b>	<b>Using the Estimated Regression Equation for Estimation and Prediction</b>	<b>631</b>
	Interval Estimation	632
	Confidence Interval for the Mean Value of $y$	633
	Prediction Interval for an Individual Value of $y$	634
<b>14.7</b>	<b>Computer Solution</b>	<b>639</b>
<b>14.8</b>	<b>Residual Analysis: Validating Model Assumptions</b>	<b>643</b>
	Residual Plot Against $x$	644
	Residual Plot Against $\hat{y}$	645
	Standardized Residuals	647
	Normal Probability Plot	649
<b>14.9</b>	<b>Residual Analysis: Outliers and Influential Observations</b>	<b>652</b>
	Detecting Outliers	652
	Detecting Influential Observations	654
	<b>Summary</b>	<b>660</b>
	<b>Glossary</b>	<b>661</b>
	<b>Key Formulas</b>	<b>662</b>
	<b>Supplementary Exercises</b>	<b>664</b>
	<b>Case Problem 1 Measuring Stock Market Risk</b>	<b>670</b>
	<b>Case Problem 2 U.S. Department of Transportation</b>	<b>671</b>
	<b>Case Problem 3 Selecting a Point-and-Shoot Digital Camera</b>	<b>672</b>
	<b>Case Problem 4 Finding the Best Car Value</b>	<b>673</b>
	<b>Case Problem 5 Buckeye Creek Amusement Park</b>	<b>674</b>
	<b>Appendix 14.1 Calculus-Based Derivation of Least Squares Formulas</b>	<b>675</b>
	<b>Appendix 14.2 A Test for Significance Using Correlation</b>	<b>676</b>
	<b>Appendix 14.3 Regression Analysis with Minitab</b>	<b>677</b>
	<b>Appendix 14.4 Regression Analysis with Excel</b>	<b>678</b>
	<b>Chapter 15 Multiple Regression</b>	<b>681</b>
	<b>Statistics in Practice: dunnhumby</b>	<b>682</b>
<b>15.1</b>	<b>Multiple Regression Model</b>	<b>683</b>
	Regression Model and Regression Equation	683
	Estimated Multiple Regression Equation	683

**15.2 Least Squares Method 684**

An Example: Butler Trucking Company 685

Note on Interpretation of Coefficients 688

**15.3 Multiple Coefficient of Determination 694****15.4 Model Assumptions 697****15.5 Testing for Significance 699***F* Test 699*t* Test 702

Multicollinearity 703

**15.6 Using the Estimated Regression Equation for Estimation and Prediction 706****15.7 Categorical Independent Variables 709**

An Example: Johnson Filtration, Inc. 709

Interpreting the Parameters 711

More Complex Categorical Variables 713

**15.8 Residual Analysis 718**

Detecting Outliers 720

Studentized Deleted Residuals and Outliers 720

Influential Observations 721

Using Cook's Distance Measure to Identify Influential Observations 721

**15.9 Logistic Regression 725**

Logistic Regression Equation 726

Estimating the Logistic Regression Equation 727

Testing for Significance 730

Managerial Use 730

Interpreting the Logistic Regression Equation 731

Logit Transformation 734

**Summary 738****Glossary 738****Key Formulas 739****Supplementary Exercises 741****Case Problem 1 Consumer Research, Inc. 748****Case Problem 2 Predicting Winnings for NASCAR Drivers 749****Case Problem 3 Finding the Best Car Value 750****Appendix 15.1 Multiple Regression with Minitab 751****Appendix 15.2 Multiple Regression with Excel 751****Appendix 15.3 Logistic Regression with Minitab 753****Chapter 16 Regression Analysis: Model Building 754****Statistics in Practice: Monsanto Company 755****16.1 General Linear Model 756**

Modeling Curvilinear Relationships 756

Interaction 759

Transformations Involving the Dependent Variable	763
Nonlinear Models That Are Intrinsically Linear	767
<b>16.2 Determining When to Add or Delete Variables</b>	<b>771</b>
General Case	773
Use of $p$ -Values	774
<b>16.3 Analysis of a Larger Problem</b>	<b>780</b>
<b>16.4 Variable Selection Procedures</b>	<b>782</b>
Stepwise Regression	782
Forward Selection	784
Backward Elimination	784
Best-Subsets Regression	785
Making the Final Choice	786
<b>16.5 Multiple Regression Approach to Experimental Design</b>	<b>788</b>
<b>16.6 Autocorrelation and the Durbin-Watson Test</b>	<b>793</b>
<b>Summary</b>	<b>797</b>
<b>Glossary</b>	<b>798</b>
<b>Key Formulas</b>	<b>798</b>
<b>Supplementary Exercises</b>	<b>798</b>
<b>Case Problem 1 Analysis of PGA Tour Statistics</b>	<b>801</b>
<b>Case Problem 2 Rating Wines from the Piedmont Region of Italy</b>	<b>802</b>
<b>Appendix 16.1 Variable Selection Procedures with Minitab</b>	<b>803</b>
<b>Chapter 17 Time Series Analysis and Forecasting</b>	<b>805</b>
<b>Statistics in Practice: Nevada Occupational Health Clinic</b>	<b>806</b>
<b>17.1 Time Series Patterns</b>	<b>807</b>
Horizontal Pattern	807
Trend Pattern	809
Seasonal Pattern	809
Trend and Seasonal Pattern	810
Cyclical Pattern	810
Selecting a Forecasting Method	812
<b>17.2 Forecast Accuracy</b>	<b>813</b>
<b>17.3 Moving Averages and Exponential Smoothing</b>	<b>818</b>
Moving Averages	818
Weighted Moving Averages	821
Exponential Smoothing	821
<b>17.4 Trend Projection</b>	<b>828</b>
Linear Trend Regression	828
Nonlinear Trend Regression	833
<b>17.5 Seasonality and Trend</b>	<b>839</b>
Seasonality Without Trend	839
Seasonality and Trend	841
Models Based on Monthly Data	844

**17.6 Time Series Decomposition 848**

Calculating the Seasonal Indexes 849

Deseasonalizing the Time Series 853

Using the Deseasonalized Time Series to Identify Trend 853

Seasonal Adjustments 855

Models Based on Monthly Data 855

Cyclical Component 855

**Summary 858****Glossary 859****Key Formulas 860****Supplementary Exercises 860****Case Problem 1 Forecasting Food and Beverage Sales 864****Case Problem 2 Forecasting Lost Sales 865****Appendix 17.1 Forecasting with Minitab 866****Appendix 17.2 Forecasting with Excel 869****Chapter 18 Nonparametric Methods 871****Statistics in Practice: West Shell Realtors 872****18.1 Sign Test 873**

Hypothesis Test About a Population Median 873

Hypothesis Test with Matched Samples 878

**18.2 Wilcoxon Signed-Rank Test 881****18.3 Mann-Whitney-Wilcoxon Test 886****18.4 Kruskal-Wallis Test 897****18.5 Rank Correlation 901****Summary 906****Glossary 906****Key Formulas 907****Supplementary Exercises 908****Appendix 18.1 Nonparametric Methods with Minitab 911****Appendix 18.2 Nonparametric Methods with Excel 913****Chapter 19 Statistical Methods for Quality Control 916****Statistics in Practice: Dow Chemical Company 917****19.1 Philosophies and Frameworks 918**

Malcolm Baldrige National Quality Award 919

ISO 9000 919

Six Sigma 919

Quality in the Service Sector 922

**19.2 Statistical Process Control 922**

Control Charts 923

 $\bar{x}$  Chart: Process Mean and Standard Deviation Known 924

$\bar{x}$  Chart: Process Mean and Standard Deviation Unknown 926  
*R* Chart 929  
*p* Chart 931  
*np* Chart 933  
 Interpretation of Control Charts 933

### **19.3 Acceptance Sampling 936**

KALI, Inc.: An Example of Acceptance Sampling 937  
 Computing the Probability of Accepting a Lot 938  
 Selecting an Acceptance Sampling Plan 941  
 Multiple Sampling Plans 943

**Summary 944**

**Glossary 944**

**Key Formulas 945**

**Supplementary Exercises 946**

**Appendix 19.1 Control Charts with Minitab 948**

## **Chapter 20 Index Numbers 950**

**Statistics in Practice: U.S. Department of Labor, Bureau of Labor Statistics 951**

**20.1 Price Relatives 952**

**20.2 Aggregate Price Indexes 952**

**20.3 Computing an Aggregate Price Index from Price Relatives 956**

**20.4 Some Important Price Indexes 958**

Consumer Price Index 958

Producer Price Index 958

Dow Jones Averages 959

**20.5 Deflating a Series by Price Indexes 960**

**20.6 Price Indexes: Other Considerations 963**

Selection of Items 963

Selection of a Base Period 963

Quality Changes 964

**20.7 Quantity Indexes 964**

**Summary 966**

**Glossary 966**

**Key Formulas 967**

**Supplementary Exercises 967**

## **Chapter 21 Decision Analysis (On Website)**

**Statistics in Practice: Ohio Edison Company 21-2**

**21.1 Problem Formulation 21-3**

Payoff Tables 21-4

Decision Trees 21-4

**21.2 Decision Making with Probabilities 21-5**

Expected Value Approach	21-5
Expected Value of Perfect Information	21-7
<b>21.3 Decision Analysis with Sample Information</b>	<b>21-13</b>
Decision Tree	21-14
Decision Strategy	21-15
Expected Value of Sample Information	21-18
<b>21.4 Computing Branch Probabilities Using Bayes' Theorem</b>	<b>21-24</b>
<b>Summary</b>	<b>21-28</b>
<b>Glossary</b>	<b>21-29</b>
<b>Key Formulas</b>	<b>21-30</b>
<b>Supplementary Exercises</b>	<b>21-30</b>
<b>Case Problem Lawsuit Defense Strategy</b>	<b>21-33</b>
<b>Appendix: Self-Test Solutions and Answers to Even-Numbered Exercises</b>	<b>21-34</b>

## **Chapter 22** Sample Survey (On Website)

<b>Statistics in Practice: Duke Energy</b>	<b>22-2</b>
<b>22.1 Terminology Used in Sample Surveys</b>	<b>22-2</b>
<b>22.2 Types of Surveys and Sampling Methods</b>	<b>22-3</b>
<b>22.3 Survey Errors</b>	<b>22-5</b>
Nonsampling Error	22-5
Sampling Error	22-5
<b>22.4 Simple Random Sampling</b>	<b>22-6</b>
Population Mean	22-6
Population Total	22-7
Population Proportion	22-8
Determining the Sample Size	22-9
<b>22.5 Stratified Simple Random Sampling</b>	<b>22-12</b>
Population Mean	22-12
Population Total	22-14
Population Proportion	22-15
Determining the Sample Size	22-16
<b>22.6 Cluster Sampling</b>	<b>22-21</b>
Population Mean	22-23
Population Total	22-25
Population Proportion	22-25
Determining the Sample Size	22-27
<b>22.7 Systematic Sampling</b>	<b>22-29</b>
<b>Summary</b>	<b>22-29</b>
<b>Glossary</b>	<b>22-30</b>
<b>Key Formulas</b>	<b>22-30</b>
<b>Supplementary Exercises</b>	<b>22-34</b>

<b>Appendix A</b>	<b>References and Bibliography</b>	<b>972</b>
<b>Appendix B</b>	<b>Tables</b>	<b>974</b>
<b>Appendix C</b>	<b>Summation Notation</b>	<b>1001</b>
<b>Appendix D</b>	<b>Self-Test Solutions and Answers to Even-Numbered Exercises</b>	<b>1003</b>
<b>Appendix E</b>	<b>Microsoft Excel 2013 and Tools for Statistical Analysis</b>	<b>1070</b>
<b>Appendix F</b>	<b>Computing <math>p</math>-Values Using Minitab and Excel</b>	<b>1078</b>
<b>Index</b>		<b>1082</b>



# Preface

This text is the 13th edition of *STATISTICS FOR BUSINESS AND ECONOMICS*.

The purpose of *Statistics for Business and Economics* is to give students, primarily those in the fields of business administration and economics, a conceptual introduction to the field of statistics and its many applications. The text is applications oriented and written with the needs of the nonmathematician in mind; the mathematical prerequisite is knowledge of algebra.

Applications of data analysis and statistical methodology are an integral part of the organization and presentation of the text material. The discussion and development of each technique is presented in an application setting, with the statistical results providing insights to decisions and solutions to problems.

Although the book is applications oriented, we have taken care to provide sound methodological development and to use notation that is generally accepted for the topic being covered. Hence, students will find that this text provides good preparation for the study of more advanced statistical material. A bibliography to guide further study is included as an appendix.

The text introduces the student to the software packages of Minitab 17 and Microsoft® Office Excel 2013 and emphasizes the role of computer software in the application of statistical analysis. Minitab is illustrated as it is one of the leading statistical software packages for both education and statistical practice. Excel is not a statistical software package, but the wide availability and use of Excel make it important for students to understand the statistical capabilities of this package. Minitab and Excel procedures are provided in appendixes so that instructors have the flexibility of using as much computer emphasis as desired for the course.

## Changes in the Thirteenth Edition

We appreciate the acceptance and positive response to the previous editions of *Statistics for Business and Economics*. Accordingly, in making modifications for this new edition, we have maintained the presentation style and readability of those editions. There have been many changes made throughout the text to enhance its educational effectiveness. The most substantial changes in the new edition are summarized here.

### Content Revisions

- **Data and Statistics—Chapter 1.** We have expanded our section on data mining to include a discussion of big data. We have added a new section on analytics. We have also placed greater emphasis on the distinction between observed and experimental data.
- **Descriptive Statistics: Tabular and Graphical Displays—Chapter 2.** We have added instructions on how to use Excel's recommended charts option to Appendix 2.2 at the end of this chapter. This new Excel functionality produces a gallery of suggested charts based on the data selected by the user and can help students identify the most appropriate chart(s) to use to depict their data.
- **Descriptive Statistics: Numerical Measures—Chapter 3.** We now use the method for calculating percentiles that is recommended by the National Institute of Standards and Technology (NIST). In addition to being the standard recommended by NIST, this approach is also used by a wide variety of software. The NIST recommended approach for calculating percentiles is used throughout the textbook.

wherever percentiles are used (for example, when creating a box plot or when calculating quantiles or an interquartile range).

- **Introduction to Probability—Chapter 4.** The discussion on experiments has been updated to draw a more clear distinction between random and designed experiments. This distinction makes it easier to understand the differences in the discussion of experiments in the probability chapters (Chapters 4, 5, and 6) and the experimental design chapter (Chapter 13).
- **Software.** We have revised all step-by-step instructions in the software appendices and all figures throughout the book that feature software output to reflect Excel 2013 and Minitab 17. This provides students exposure to and experience with the current versions of two of the most commonly used software for statistical analysis in business. In this latest edition, we no longer provide discussion of the use of StatTools.
- **Case Problems.** We have added two new case problems in this addition; the total number of cases is 33. One new probability modeling case has been added to Chapter 5, and one new simple linear regression case appears in Chapter 14. The 33 case problems in this book provide students the opportunity to work on more complex problems, analyze larger data sets, and prepare managerial reports based on the results of their analyses.
- **Examples and Exercises Based on Real Data.** We continue to make a substantial effort to update our text examples and exercises with the most current real data and referenced sources of statistical information. In this edition, we have added more than 180 new examples and exercises based on real data and referenced sources. Using data from sources also used by *The Wall Street Journal*, *USA Today*, *Barron's*, and others, we have drawn from actual studies and applications to develop explanations and create exercises that demonstrate the many uses of statistics in business and economics. We believe that the use of real data from interesting and relevant problems helps generate more student interest in the material and enables the student to learn about both statistical methodology and its application. The 13th edition contains more than 350 examples and exercises based on real data.

## Features and Pedagogy

Authors Anderson, Sweeney, Williams, Camm, and Cochran have continued many of the features that appeared in previous editions. Important ones for students are noted here.

### Methods Exercises and Applications Exercises

The end-of-section exercises are split into two parts, Methods and Applications. The Methods exercises require students to use the formulas and make the necessary computations. The Applications exercises require students to use the chapter material in real-world situations. Thus, students first focus on the computational “nuts and bolts” and then move on to the subtleties of statistical application and interpretation.

### Self-Test Exercises

Certain exercises are identified as “Self-Test Exercises.” Completely worked-out solutions for these exercises are provided in Appendix D. Students can attempt the Self-Test Exercises and immediately check the solution to evaluate their understanding of the concepts presented in the chapter.

### Margin Annotations and Notes and Comments

Margin annotations that highlight key points and provide additional insights for the student are a key feature of this text. These annotations, which appear in the margins, are designed

to provide emphasis and enhance understanding of the terms and concepts being presented in the text.

At the end of many sections, we provide Notes and Comments designed to give the student additional insights about the statistical methodology and its application. Notes and Comments include warnings about or limitations of the methodology, recommendations for application, brief descriptions of additional technical considerations, and other matters.

## Data Files Accompany the Text

Over 200 data files are available on the website that accompanies the text. In previous editions, we provided data files in both Excel and Minitab formats. In this edition, to be more efficient, we provide the data files in only one format, CSV (comma separated values). In the appendices to Chapter 2, we provide instructions on how to open CSV files in both Excel and Minitab. DATAfile logos are used in the text to identify the data sets that are available on the website. Data sets for all case problems as well as data sets for larger exercises are included. In this edition, instead of supplying both Minitab and Excel data files, we provide data files in a single format (CSV format). This format is accessible to both Minitab and Excel. We give step-by-step instructions on how to open these files in Minitab and Excel in Appendices 2.1 and 2.2 at the end of Chapter 2.

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# CHAPTER 1

## Data and Statistics

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### CONTENTS

#### STATISTICS IN PRACTICE:

#### *BLOOMBERG BUSINESSWEEK*

#### 1.1 APPLICATIONS IN BUSINESS AND ECONOMICS

Accounting

Finance

Marketing

Production

Economics

Information Systems

#### 1.2 DATA

Elements, Variables,  
and Observations

Scales of Measurement

Categorical and

Quantitative Data

Cross-Sectional and Time

Series Data

#### 1.3 DATA SOURCES

Existing Sources

Observational Study

Experiment

Time and Cost Issues

Data Acquisition Errors

#### 1.4 DESCRIPTIVE STATISTICS

#### 1.5 STATISTICAL INFERENCE

#### 1.6 ANALYTICS

#### 1.7 BIG DATA AND DATA MINING

#### 1.8 COMPUTERS AND STATISTICAL ANALYSIS

#### 1.9 ETHICAL GUIDELINES FOR STATISTICAL PRACTICE

## STATISTICS *in* PRACTICE

### *BLOOMBERG BUSINESSWEEK\** NEW YORK, NEW YORK

With a global circulation of more than 1 million, *Bloomberg Businessweek* is one of the most widely read business magazines in the world. Bloomberg's 1700 reporters in 145 service bureaus around the world enable *Bloomberg Businessweek* to deliver a variety of articles of interest to the global business and economic community. Along with feature articles on current topics, the magazine contains articles on international business, economic analysis, information processing, and science and technology. Information in the feature articles and the regular sections helps readers stay abreast of current developments and assess the impact of those developments on business and economic conditions.

Most issues of *Bloomberg Businessweek*, formerly *BusinessWeek*, provide an in-depth report on a topic of current interest. Often, the in-depth reports contain statistical facts and summaries that help the reader understand the business and economic information. Examples of articles and reports include the impact of businesses moving important work to cloud computing, the crisis facing the U.S. Postal Service, and why the debt crisis is even worse than we think. In addition, *Bloomberg Businessweek* provides a variety of statistics about the state of the economy, including production indexes, stock prices, mutual funds, and interest rates.

*Bloomberg Businessweek* also uses statistics and statistical information in managing its own business. For example, an annual survey of subscribers helps the company learn about subscriber demographics, reading habits, likely purchases, lifestyles, and so on. *Bloomberg Businessweek* managers use statistical summaries from the survey to provide better services to subscribers and advertisers. One recent North American subscriber survey indicated that 90% of *Bloomberg Businessweek*

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*Bloomberg Businessweek* uses statistical facts and summaries in many of its articles.

subscribers use a personal computer at home and that 64% of *Bloomberg Businessweek* subscribers are involved with computer purchases at work. Such statistics alert *Bloomberg Businessweek* managers to subscriber interest in articles about new developments in computers. The results of the subscriber survey are also made available to potential advertisers. The high percentage of subscribers using personal computers at home and the high percentage of subscribers involved with computer purchases at work would be an incentive for a computer manufacturer to consider advertising in *Bloomberg Businessweek*.

In this chapter, we discuss the types of data available for statistical analysis and describe how the data are obtained. We introduce descriptive statistics and statistical inference as ways of converting data into meaningful and easily interpreted statistical information.

Frequently, we see the following types of statements in newspapers and magazines:

- Against the U.S. dollar, the euro has lost nearly 30% of its value in the last year; the Australian dollar lost almost 20% (*The Economist*, April 25th–May 1st, 2015).
- A survey conducted by the Pew Research Center reported that 68% of Internet users believe current laws are not good enough in protecting people's privacy online (*The Wall Street Journal*, March 24, 2014).

- VW Group's U.S. sales continue to slide, with total sales off by 13% from last January, to 36,930 vehicles (*Panorama*, March 2014).
- A poll of 1,320 corporate recruiters indicated that 68% of the recruiters ranked communication skills as one of the top five most important skills for new hires (*Bloomberg Businessweek* April 13–April 19, 2015).
- The California State Teachers' Retirement System has \$154.3 billion under management (*Bloomberg Businessweek*, January 21–January 27, 2013).
- At a Sotheby's art auction held on February 5, 2013, Pablo Picasso's painting *Woman Sitting Near a Window* sold for \$45 million (*The Wall Street Journal*, February 15, 2013).
- Over the past three months, the industry average for sales incentives per vehicle by GM, Chrysler, Ford, Toyota, and Honda was \$2336 (*The Wall Street Journal*, February 14, 2013).

The numerical facts in the preceding statements—30%, 20%, 68%, 13%, 36,930, 1320, 68%, \$154.3 billion, \$45 million, \$2336—are called **statistics**. In this usage, the term *statistics* refers to numerical facts such as averages, medians, percentages, and maximums that help us understand a variety of business and economic situations. However, as you will see, the field, or subject, of statistics involves much more than numerical facts. In a broader sense, statistics is the art and science of collecting, analyzing, presenting, and interpreting data. Particularly in business and economics, the information provided by collecting, analyzing, presenting, and interpreting data gives managers and decision makers a better understanding of the business and economic environment and thus enables them to make more informed and better decisions. In this text, we emphasize the use of statistics for business and economic decision making.

Chapter 1 begins with some illustrations of the applications of statistics in business and economics. In Section 1.2 we define the term *data* and introduce the concept of a data set. This section also introduces key terms such as *variables* and *observations*, discusses the difference between quantitative and categorical data, and illustrates the uses of cross-sectional and time series data. Section 1.3 discusses how data can be obtained from existing sources or through survey and experimental studies designed to obtain new data. The important role that the Internet now plays in obtaining data is also highlighted. The uses of data in developing descriptive statistics and in making statistical inferences are described in Sections 1.4 and 1.5. The last four sections of Chapter 1 provide an introduction to business analytics and the role statistics plays in it, an introduction to big data and data mining, the role of the computer in statistical analysis, and a discussion of ethical guidelines for statistical practice.

## 1.1

# Applications in Business and Economics

In today's global business and economic environment, anyone can access vast amounts of statistical information. The most successful managers and decision makers understand the information and know how to use it effectively. In this section, we provide examples that illustrate some of the uses of statistics in business and economics.

## Accounting

Public accounting firms use statistical sampling procedures when conducting audits for their clients. For instance, suppose an accounting firm wants to determine whether the amount of accounts receivable shown on a client's balance sheet fairly represents the actual amount of accounts receivable. Usually the large number of individual accounts receivable makes

reviewing and validating every account too time-consuming and expensive. As common practice in such situations, the audit staff selects a subset of the accounts called a sample. After reviewing the accuracy of the sampled accounts, the auditors draw a conclusion as to whether the accounts receivable amount shown on the client's balance sheet is acceptable.

## Finance

Financial analysts use a variety of statistical information to guide their investment recommendations. In the case of stocks, analysts review financial data such as price/earnings ratios and dividend yields. By comparing the information for an individual stock with information about the stock market averages, an analyst can begin to draw a conclusion as to whether the stock is a good investment. For example, *The Wall Street Journal* (June 6, 2015) reported that the average dividend yield for the S&P 500 companies was 2%. Microsoft showed a dividend yield of 1.95%. In this case, the statistical information on dividend yield indicates a lower dividend yield for Microsoft than the average dividend yield for the S&P 500 companies. This and other information about Microsoft would help the analyst make an informed buy, sell, or hold recommendation for Microsoft stock.

## Marketing

Electronic scanners at retail checkout counters collect data for a variety of marketing research applications. For example, data suppliers such as ACNielsen and Information Resources, Inc., purchase point-of-sale scanner data from grocery stores, process the data, and then sell statistical summaries of the data to manufacturers. Manufacturers spend hundreds of thousands of dollars per product category to obtain this type of scanner data. Manufacturers also purchase data and statistical summaries on promotional activities such as special pricing and the use of in-store displays. Brand managers can review the scanner statistics and the promotional activity statistics to gain a better understanding of the relationship between promotional activities and sales. Such analyses often prove helpful in establishing future marketing strategies for the various products.

## Production

Today's emphasis on quality makes quality control an important application of statistics in production. A variety of statistical quality control charts are used to monitor the output of a production process. In particular, an  $\bar{x}$ -bar chart can be used to monitor the average output. Suppose, for example, that a machine fills containers with 12 ounces of a soft drink. Periodically, a production worker selects a sample of containers and computes the average number of ounces in the sample. This average, or  $\bar{x}$ -bar value, is plotted on an  $\bar{x}$ -bar chart. A plotted value above the chart's upper control limit indicates overfilling, and a plotted value below the chart's lower control limit indicates underfilling. The process is termed "in control" and allowed to continue as long as the plotted  $\bar{x}$ -bar values fall between the chart's upper and lower control limits. Properly interpreted, an  $\bar{x}$ -bar chart can help determine when adjustments are necessary to correct a production process.

## Economics

Economists frequently provide forecasts about the future of the economy or some aspect of it. They use a variety of statistical information in making such forecasts. For instance, in forecasting inflation rates, economists use statistical information on such indicators as the Producer Price Index, the unemployment rate, and manufacturing capacity utilization. Often these statistical indicators are entered into computerized forecasting models that predict inflation rates.

## Information Systems

Information systems administrators are responsible for the day-to-day operation of an organization's computer networks. A variety of statistical information helps administrators assess the performance of computer networks, including local area networks (LANs), wide area networks (WANs), network segments, intranets, and other data communication systems. Statistics such as the mean number of users on the system, the proportion of time any component of the system is down, and the proportion of bandwidth utilized at various times of the day are examples of statistical information that help the system administrator better understand and manage the computer network.

Applications of statistics such as those described in this section are an integral part of this text. Such examples provide an overview of the breadth of statistical applications. To supplement these examples, practitioners in the fields of business and economics provided chapter-opening Statistics in Practice articles that introduce the material covered in each chapter. The Statistics in Practice applications show the importance of statistics in a wide variety of business and economic situations.

### 1.2

## Data

**Data** are the facts and figures collected, analyzed, and summarized for presentation and interpretation. All the data collected in a particular study are referred to as the **data set** for the study. Table 1.1 shows a data set containing information for 60 nations that participate in the World Trade Organization. The World Trade Organization encourages the free flow of international trade and provides a forum for resolving trade disputes.

### Elements, Variables, and Observations

**Elements** are the entities on which data are collected. Each nation listed in Table 1.1 is an element with the nation or element name shown in the first column. With 60 nations, the data set contains 60 elements.

A **variable** is a characteristic of interest for the elements. The data set in Table 1.1 includes the following five variables:

- **WTO Status:** The nation's membership status in the World Trade Organization; this can be either as a member or an observer.
- **Per Capita GDP (\$):** The total market value (\$) of all goods and services produced by the nation divided by the number of people in the nation; this is commonly used to compare economic productivity of the nations.
- **Trade Deficit (\$1000s):** The difference between the total dollar value of the nation's imports and the total dollar value of the nation's exports.
- **Fitch Rating:** The nation's sovereign credit rating as appraised by the Fitch Group<sup>1</sup>; the credit ratings range from a high of AAA to a low of F and can be modified by + or -.
- **Fitch Outlook:** An indication of the direction the credit rating is likely to move over the upcoming two years; the outlook can be negative, stable, or positive.

Measurements collected on each variable for every element in a study provide the data. The set of measurements obtained for a particular element is called an **observation**. Referring to Table 1.1, we see that the first observation (Armenia) contains the following measurements:

<sup>1</sup>The Fitch Group is one of three nationally recognized statistical rating organizations designated by the U.S. Securities and Exchange Commission. The other two are Standard and Poor's and Moody's investor service.

**TABLE 1.1** DATA SET FOR 60 NATIONS IN THE WORLD TRADE ORGANIZATION

**DATA file**  
Nations

*Data sets such as Nations are available on the website for this text.*

Nation	WTO Status	Per Capita GDP (\$)	Trade Deficit (\$1000s)	Fitch Rating	Fitch Outlook
Armenia	Member	5,400	2,673,359	BB-	Stable
Australia	Member	40,800	-33,304,157	AAA	Stable
Austria	Member	41,700	12,796,558	AAA	Stable
Azerbaijan	Observer	5,400	-16,747,320	BBB-	Positive
Bahrain	Member	27,300	3,102,665	BBB	Stable
Belgium	Member	37,600	-14,930,833	AA+	Negative
Brazil	Member	11,600	-29,796,166	BBB	Stable
Bulgaria	Member	13,500	4,049,237	BBB-	Positive
Canada	Member	40,300	-1,611,380	AAA	Stable
Cape Verde	Member	4,000	874,459	B+	Stable
Chile	Member	16,100	-14,558,218	A+	Stable
China	Member	8,400	-156,705,311	A+	Stable
Colombia	Member	10,100	-1,561,199	BBB-	Stable
Costa Rica	Member	11,500	5,807,509	BB+	Stable
Croatia	Member	18,300	8,108,103	BBB-	Negative
Cyprus	Member	29,100	6,623,337	BBB	Negative
Czech Republic	Member	25,900	-10,749,467	A+	Positive
Denmark	Member	40,200	-15,057,343	AAA	Stable
Ecuador	Member	8,300	1,993,819	B-	Stable
Egypt	Member	6,500	28,486,933	BB	Negative
El Salvador	Member	7,600	5,019,363	BB	Stable
Estonia	Member	20,200	802,234	A+	Stable
France	Member	35,000	118,841,542	AAA	Stable
Georgia	Member	5,400	4,398,153	B+	Positive
Germany	Member	37,900	-213,367,685	AAA	Stable
Hungary	Member	19,600	-9,421,301	BBB-	Negative
Iceland	Member	38,000	-504,939	BB+	Stable
Ireland	Member	39,500	-59,093,323	BBB+	Negative
Israel	Member	31,000	6,722,291	A	Stable
Italy	Member	30,100	33,568,668	A+	Negative
Japan	Member	34,300	31,675,424	AA	Negative
Kazakhstan	Observer	13,000	-33,220,437	BBB	Positive
Kenya	Member	1,700	9,174,198	B+	Stable
Latvia	Member	15,400	2,448,053	BBB-	Positive
Lebanon	Observer	15,600	13,715,550	B	Stable
Lithuania	Member	18,700	3,359,641	BBB	Positive
Malaysia	Member	15,600	-39,420,064	A-	Stable
Mexico	Member	15,100	1,288,112	BBB	Stable
Peru	Member	10,000	-7,888,993	BBB	Stable
Philippines	Member	4,100	15,667,209	BB+	Stable
Poland	Member	20,100	19,552,976	A-	Stable
Portugal	Member	23,200	21,060,508	BBB-	Negative
South Korea	Member	31,700	-37,509,141	A+	Stable
Romania	Member	12,300	13,323,709	BBB-	Stable
Russia	Observer	16,700	-151,400,000	BBB	Positive
Rwanda	Member	1,300	939,222	B	Stable
Serbia	Observer	10,700	8,275,693	BB-	Stable
Seychelles	Observer	24,700	666,026	B	Stable
Singapore	Member	59,900	-27,110,421	AAA	Stable
Slovakia	Member	23,400	-2,110,626	A+	Stable
Slovenia	Member	29,100	2,310,617	AA-	Negative



South Africa	Member	11,000	3,321,801	BBB+	Stable
Sweden	Member	40,600	−10,903,251	AAA	Stable
Switzerland	Member	43,400	−27,197,873	AAA	Stable
Thailand	Member	9,700	2,049,669	BBB	Stable
Turkey	Member	14,600	71,612,947	BB+	Positive
UK	Member	35,900	162,316,831	AAA	Negative
Uruguay	Member	15,400	2,662,628	BB	Positive
USA	Member	48,100	784,438,559	AAA	Stable
Zambia	Member	1,600	−1,805,198	B+	Stable

Member, 5,400, 2,673,359, BB−, and Stable. The second observation (Australia) contains the following measurements: Member, 40,800, −33,304,157, AAA, Stable, and so on. A data set with 60 elements contains 60 observations.

## Scales of Measurement

Data collection requires one of the following scales of measurement: nominal, ordinal, interval, or ratio. The scale of measurement determines the amount of information contained in the data and indicates the most appropriate data summarization and statistical analyses.

When the data for a variable consist of labels or names used to identify an attribute of the element, the scale of measurement is considered a **nominal scale**. For example, referring to the data in Table 1.1, the scale of measurement for the WTO Status variable is nominal because the data “member” and “observer” are labels used to identify the status category for the nation. In cases where the scale of measurement is nominal, a numerical code as well as a nonnumerical label may be used. For example, to facilitate data collection and to prepare the data for entry into a computer database, we might use a numerical code for the WTO Status variable by letting 1 denote a member nation in the World Trade Organization and 2 denote an observer nation. The scale of measurement is nominal even though the data appear as numerical values.

The scale of measurement for a variable is considered an **ordinal scale** if the data exhibit the properties of nominal data and in addition, the order or rank of the data is meaningful. For example, referring to the data in Table 1.1, the scale of measurement for the Fitch Rating is ordinal because the rating labels which range from AAA to F can be rank ordered from best credit rating AAA to poorest credit rating F. The rating letters provide the labels similar to nominal data, but in addition, the data can also be ranked or ordered based on the credit rating, which makes the measurement scale ordinal. Ordinal data can also be recorded by a numerical code, for example, your class rank in school.

The scale of measurement for a variable is an **interval scale** if the data have all the properties of ordinal data and the interval between values is expressed in terms of a fixed unit of measure. Interval data are always numerical. College admission SAT scores are an example of interval-scaled data. For example, three students with SAT math scores of 620, 550, and 470 can be ranked or ordered in terms of best performance to poorest performance in math. In addition, the differences between the scores are meaningful. For instance, student 1 scored  $620 - 550 = 70$  points more than student 2, while student 2 scored  $550 - 470 = 80$  points more than student 3.

The scale of measurement for a variable is a **ratio scale** if the data have all the properties of interval data and the ratio of two values is meaningful. Variables such as distance, height, weight, and time use the ratio scale of measurement. This scale requires that a zero value be included to indicate that nothing exists for the variable at the zero point.

For example, consider the cost of an automobile. A zero value for the cost would indicate that the automobile has no cost and is free. In addition, if we compare the cost of \$30,000 for one automobile to the cost of \$15,000 for a second automobile, the ratio property shows that the first automobile is  $\$30,000/\$15,000 = 2$  times, or twice, the cost of the second automobile.

## Categorical and Quantitative Data

Data can be classified as either categorical or quantitative. Data that can be grouped by specific categories are referred to as **categorical data**. Categorical data use either the nominal or ordinal scale of measurement. Data that use numeric values to indicate how much or how many are referred to as **quantitative data**. Quantitative data are obtained using either the interval or ratio scale of measurement.

A **categorical variable** is a variable with categorical data, and a **quantitative variable** is a variable with quantitative data. The statistical analysis appropriate for a particular variable depends upon whether the variable is categorical or quantitative. If the variable is categorical, the statistical analysis is limited. We can summarize categorical data by counting the number of observations in each category or by computing the proportion of the observations in each category. However, even when the categorical data are identified by a numerical code, arithmetic operations such as addition, subtraction, multiplication, and division do not provide meaningful results. Section 2.1 discusses ways of summarizing categorical data.

Arithmetic operations provide meaningful results for quantitative variables. For example, quantitative data may be added and then divided by the number of observations to compute the average value. This average is usually meaningful and easily interpreted. In general, more alternatives for statistical analysis are possible when data are quantitative. Section 2.2 and Chapter 3 provide ways of summarizing quantitative data.

## Cross-Sectional and Time Series Data

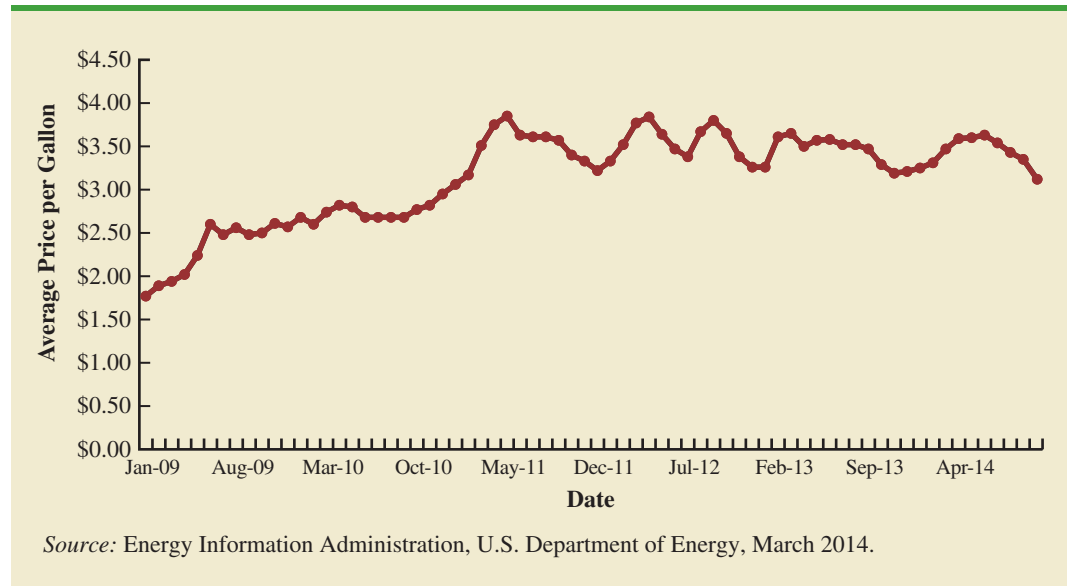
For purposes of statistical analysis, distinguishing between cross-sectional data and time series data is important. **Cross-sectional data** are data collected at the same or approximately the same point in time. The data in Table 1.1 are cross-sectional because they describe the five variables for the 60 World Trade Organization nations at the same point in time. **Time series data** are data collected over several time periods. For example, the time series in Figure 1.1 shows the U.S. average price per gallon of conventional regular gasoline between 2009 and 2014. Between January 2009 and May 2011, the average price per gallon continued to climb steadily. Since then prices have shown more fluctuation, reaching an average price per gallon of \$3.12 in October 2014.

Graphs of time series data are frequently found in business and economic publications. Such graphs help analysts understand what happened in the past, identify any trends over time, and project future values for the time series. The graphs of time series data can take on a variety of forms, as shown in Figure 1.2. With a little study, these graphs are usually easy to understand and interpret. For example, Panel (A) in Figure 1.2 is a graph that shows the Dow Jones Industrial Average Index from 2004 to 2014. In November 2004, the popular stock market index was near 10,000. The index rose to slightly over 14,000 in October 2007. However, notice the sharp decline in the time series after the high in 2007. By February 2009, poor economic conditions had caused the Dow Jones Industrial Average Index to return to the 7000 level. This was a scary and discouraging period for investors. However, by late 2009, the index was showing a recovery by reaching 10,000. The index has climbed steadily since then and was above 17,500 in November 2014.

*The statistical method appropriate for summarizing data depends upon whether the data are categorical or quantitative.*



**FIGURE 1.1** U.S. AVERAGE PRICE PER GALLON FOR CONVENTIONAL REGULAR GASOLINE



The graph in Panel (B) shows the net income of McDonald's Inc. from 2005 to 2013. The declining economic conditions in 2008 and 2009 were actually beneficial to McDonald's as the company's net income rose to all-time highs. The growth in McDonald's net income showed that the company was thriving during the economic downturn as people were cutting back on the more expensive sit-down restaurants and seeking less-expensive alternatives offered by McDonald's. McDonald's net income continued to new all-time highs in 2010 and 2011, decreased slightly in 2012, and increased in 2013.

Panel (C) shows the time series for the occupancy rate of hotels in South Florida over a one-year period. The highest occupancy rates, 95% and 98%, occur during the months of February and March when the climate of South Florida is attractive to tourists. In fact, January to April of each year is typically the high-occupancy season for South Florida hotels. On the other hand, note the low occupancy rates during the months of August to October, with the lowest occupancy rate of 50% occurring in September. High temperatures and the hurricane season are the primary reasons for the drop in hotel occupancy during this period.

## NOTES AND COMMENTS

1. An observation is the set of measurements obtained for each element in a data set. Hence, the number of observations is always the same as the number of elements. The number of measurements obtained for each element equals the number of variables. Hence, the total number of data items can be determined by multiplying the number of observations by the number of variables.
2. Quantitative data may be discrete or continuous. Quantitative data that measure how many (e.g., number of calls received in 5 minutes) are discrete. Quantitative data that measure how much (e.g., weight or time) are continuous because no separation occurs between the possible data values.